## MATH 210: 1/29 WORKSHEET

For the following, determine with the expression is infinitesimal, finite but non-infinitesimal, or infinite. Here  $\varepsilon$  is infinitesimal, *a* is positive and finite, and *H* is positive and infinite.

(1) 
$$3a^2 + 3a\varepsilon + \varepsilon^2$$
  
(2)  $\frac{3}{\sqrt{\varepsilon}}$   
(3)  $\frac{\sqrt{a+\varepsilon} - \sqrt{a}}{\varepsilon}$   
(4)  $\sqrt{H+100} - \sqrt{H}$   
(5)  $\frac{3H^2 - H}{H^2 + 4}$ 

For the following, determine the standard part of the expression, or say why the standard part is undefined. Here  $\varepsilon$  is infinitesimal, *a* is positive and finite, and *H* is positive and infinite.

(1) 
$$3a^2 + 3a\varepsilon + \varepsilon^2$$
  
(2)  $\frac{3}{\sqrt{\varepsilon}}$   
(3)  $\frac{\sqrt{a+\varepsilon} - \sqrt{a}}{\varepsilon}$   
(4)  $\sqrt{H+100} - \sqrt{H}$   
(5)  $\frac{3H^2 - H}{H^2 + 4}$ 

Calculate the following limits. Here a is a positive real number.

(1) 
$$\lim_{x \to 0} 3a^2 + 3ax + x^2$$
  
(2) 
$$\lim_{x \to 0} \frac{3}{\sqrt{x}}$$
  
(3) 
$$\lim_{x \to 0} \frac{\sqrt{a+x} - \sqrt{a}}{x}$$
  
(4) 
$$\lim_{x \to \infty} \sqrt{x+100} - \sqrt{x}$$
  
(5) 
$$\lim_{x \to \infty} \frac{3x^2 - x}{x^2 + 4}$$