

MATH 302: LAPLACE TRANSFORMS

All functions in the time domain here are defined on $0 \leq t < \infty$.

$f(t)$	$\mathcal{L}[f]$	converges when
1	$\frac{1}{s}$	$s > 0$
t	$\frac{1}{s^2}$	$s > 0$
t^n	$\frac{n!}{s^{n+1}}$	$s > 0$
t^α	$\frac{\Gamma(\alpha + 1)}{s^{\alpha+1}}$	$s > 0, \alpha > -1$
e^{at}	$\frac{1}{s - a}$	$s > a$
$t^n e^{at}$	$\frac{n!}{(s - a)^{n+1}}$	$s > a$
$\sin(bt)$	$\frac{b}{s^2 + b^2}$	$s > 0$
$\cos(bt)$	$\frac{s}{s^2 + b^2}$	$s > 0$
$t \sin(bt)$	$\frac{2bs}{(s^2 + b^2)^2}$	$s > 0$
$t \cos(bt)$	$\frac{s^2 - b^2}{(s^2 + b^2)^2}$	$s > 0$
$e^{at} \sin(bt)$	$\frac{b}{(s - a)^2 + b^2}$	$s > a$
$e^{at} \cos(bt)$	$\frac{s - a}{(s - a)^2 + b^2}$	$s > a$